

Proceedings  
of the seventh South African

**SYMPOSIUM  
ON  
NUMERICAL MATHEMATICS**

Durban, 20, 21 & 22 July 1981



computer science department

university of natal

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G.R. Joubert

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## PREFACE

In 1975 the Department of Computer Science of the University of Natal organised the first South African Symposium on Numerical Mathematics in Durban. Since then these symposia have become an annual event. The seventh such symposium was held in Durban on 20, 21 and 22 July 1981.

These proceedings are a published record of most of the papers presented. The choice was left to the authors as to whether they wished to publish their papers in full or as a summary or whether they preferred only an abstract to be published. All contributions included in the proceedings are published as received from authors.

Invited papers were read by Professor G. Hämmerlin, Professor J. Whiteman, Professor R.J.Y. McLeod and Dr. H. Voss.

The symposium was again supported financially by IBM South Africa. The continued support of IBM over the past six years has made it possible regularly to invite overseas speakers who have greatly contributed to the stimulation of research in this field in South Africa and neighbouring states.

At the last symposium it was decided by the delegates to form a separate society which will take over the responsibility for the organisation of future symposia.

Appreciation and thanks are due to Pat Duminy of the Public Relations Office of the University of Natal and to Ethel Carte and Wendy Midgley of the Computer Science Department for assisting with the organisation of the symposium. Ethne de Groot of the Computer Science Department has taken on the unenviable task of preparing the proceedings.

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