

**Proceedings
of the tenth South African**

**SYMPOSIUM
ON
NUMERICAL MATHEMATICS**

Ballito 2, 3 & 4 July 1984

**sanum & the
dept. of computer science
university of natal
durban**

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JA Snyman

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PREFACE

For the three days July 2-4, 1984 numerical mathematicians of South Africa as well as two leading numerical analysts from overseas gathered in Ballito, Natal, to celebrate the special event of the Tenth South African Symposium on Numerical Mathematics. This event was organised by the South African Society for Numerical Mathematics (SANUM) in conjunction with the University of Natal. A record total of 38 papers were read at this gathering. Invited papers were presented by Dr Sean McKee of the Oxford University Consortium for Industrial Numerical Analysis and by Dr GR Joubert of Philips, Eindhoven.

The Proceedings are a published record of 33 of the papers presented. The choice was left to the authors as to whether they wished to publish their papers in full or as a summary. All contributions included in the Proceedings are published as received from the authors.

This preface provides the opportunity to thank all the speakers, chairmen of sessions and participants for their contributions. Our thanks also to the University of Natal, in particular the head of the Department of Computer Science Prof Sartori-Angus and his very able assistant Ms Ethel Carte, for helping with the organisation of the Symposium.

Financial support for this meeting was again obtained from IBM (South Africa). In times of escalating costs it would not have been possible to present this Symposium without IBM's help and this support is gratefully acknowledged.

Jan Snyman
(Vice-Chairman : SANUM)

September 1984

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